Knock Behavior of a Lean-Burn, H₂ and CO Enhanced, SI Gasoline Engine Concept

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ABSTRACT

Experiments were performed to identify the knock trends of lean hydrocarbon-air mixtures, and such mixtures enhanced with hydrogen (H₂) and carbon monoxide (CO). These enhanced mixtures simulated 15% and 30% of the engine’s gasoline being reformed in a plasmatron fuel reformer [1]. Knock trends were determined by measuring the octane number (ON) of the primary reference fuel (mixture of isoctane and n-heptane) supplied to the engine that just produced audible knock.

Experimental results show that leaner operation does not decrease the knock tendency of an engine under conditions where a fixed output torque is maintained; rather it slightly increases the octane requirement. The knock tendency does decrease with lean operation when the intake pressure is held constant, but engine torque is then reduced. When H₂ and CO are added to the mixture, the knock susceptibility is reduced, as illustrated by a decrease in the measured octane number of the primary reference fuel resulting in knock. Experiments conducted with the addition of H₂ and CO separately show similar trends, but to a lesser degree; therefore, both H₂ and CO act as octane enhancers when added to a hydrocarbon-air mixture. The extent to which H₂ and CO improve the knock resistance of a mixture can be estimated by finding the bond-weighted octane numbers for these non-traditional blends of fuels.

To understand these results better, a reduced chemical kinetic model was also used to predict autoignition of the end-gas for various conditions and fuel-air mixtures. Predicted model trends of knock onset of primary reference fuels agree with experimental observations. A comprehensive isoctane chemistry mechanism was used to demonstrate that H₂ and CO are effective in lengthening the ignition delay, thereby reducing knock tendency.

INTRODUCTION AND BACKGROUND

Knock is caused by the spontaneous ignition and rapid energy release of unburned fuel and air ahead of the propagating flame front in a spark-ignition (SI) engine [2]. This rapid release of energy causes a rise in local pressure. The pressure waves, which then propagate across the gas in the combustion chamber, cause the engine block and cylinder head to vibrate, generating a clanging or pinging noise. This noise is unattractive to drivers; in addition, extended operation under heavy knocking conditions can cause damage to engine components.

Knock has been studied for many decades, but remains a significant engine constraint. Advances in fuel processing have resulted in gasolines with increased knock resistance; in addition, fast burning combustion chamber designs help to control knock. Nevertheless, engine performance and efficiency are limited by knock onset. If new methods to control knock are developed, engine performance and efficiency could be significantly improved.

One way to suppress knock in a naturally aspirated engine is to operate the engine with excess air in the cylinder. However, under these lean operating conditions, the engine torque decreases. If the engine is boosted to maintain constant torque, then the knock tendency relative to operation with stoichiometric mixtures is unclear.

The traditional motivation for lean engine operation is to increase fuel conversion efficiency and reduce engine-out emissions. In general, the leaner the mixture, the greater the efficiency and emissions benefit. However, at some point the engine cannot support stable combustion mainly due to low flame speeds, and the lean limit is reached [3]. To extend the stable range of lean operation small amounts of hydrogen, which burns much faster than gasoline, can be added to the fuel-air mixture. To obtain
hydrogen onboard a vehicle, a fuel reformer can be used to produce a hydrogen (H₂), carbon monoxide (CO), and nitrogen (N₂) mixture from partial oxidation of a hydrocarbon with air. Several types of gasoline partial oxidation reformer systems are being developed (e.g. [4]). The concept investigated for this research uses a plasmatorn reformer [5]. The plasmatorn uses an electrical discharge to initiate the fuel reforming chemistry. Through partial oxidation of the gasoline, reformate gas of about equal concentrations of H₂ and CO, with the N₂ from the air used, and small amounts of H₂O and CO₂ is produced. The concept involves a fraction (e.g. 10% - 30%) of the gasoline being reformed in the plasmatorn fuel reformer. The hydrogen-rich stream is then mixed with the main fuel/air mixture in the intake manifold.

The work presented here explores the opportunities for suppressing knock by lean, hydrogen and CO-enhanced engine operation. The engine's Octane Number Requirement (ONR) - defined as the octane number of the fuel that just produces audible knock - indicates its propensity to knock. This work examines the changes in knock limits of an engine under lean operating conditions by examining the ONR at various operating conditions. The role of H₂ and CO on knock behavior was explored by finding the octane number improvement contributed by H₂ and CO when added to blends of primary reference fuels. The changes in knock behavior will be discussed and related to fundamental explanations using engine experiments and modeling.

Past research on lean knock limits has indicated various trends. Some literature shows that lean mixtures are more knock resistant, and therefore allow a higher compression ratio [6][7][8]. Other literature questions the assumption that lean mixtures allow for a higher compression ratio, especially at high loads [9]. This work attempts to answer the questions regarding knock trends with leaner mixtures where output torque is maintained.

**EXPERIMENTAL METHOD**

**EXPERIMENTAL SETUP** - The base engine used in this study is a single-cylinder Ricardo Hydra MK III. The engine cylinder head has been replaced with a B5254 Volvo head to better represent current engines. The spark plug is located in the center of the pentroof combustion chamber. There are four valves, which are actuated by belt-driven dual overhead camshafts. Turbulence is increased by generating swirl with a charge motion control plate in the intake port. The complete specifications of the engine are shown in Table 1. The engine is equipped with an air supply from a compressor to simulate boosted operation.

**Table 1: Engine specifications**

<table>
<thead>
<tr>
<th>Specification</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Displaced Volume (cm³)</td>
<td>487</td>
</tr>
<tr>
<td>Clearance Volume (cm³)</td>
<td>54</td>
</tr>
<tr>
<td>Bore (mm)</td>
<td>83</td>
</tr>
<tr>
<td>Stroke (mm)</td>
<td>90</td>
</tr>
<tr>
<td>Con Rod Length (mm)</td>
<td>158</td>
</tr>
<tr>
<td>Compression Ratio</td>
<td>10.1</td>
</tr>
<tr>
<td>Valve Timing</td>
<td>IVC 60° ABDC, IVO 0° ATDC, EVC 6° ATDC, EVO 68° BBDC</td>
</tr>
</tbody>
</table>

**EXPERIMENTAL PROCEDURE** - A series of experiments were performed to investigate the knock trends for mixtures of primary reference fuels, with and without the addition of H₂ and CO. All tests were completed at 1500 rpm, MBT spark timing, with coolant temperature at 90°C and intake air temperature at 20°C.

The engine parameters that were controlled and measured include the airflow and its temperature and pressure, the fuel flow rates, and the relative air/fuel ratio. The net indicated mean effective pressure (NIMEP) was calculated based on the cylinder pressure trace. The octane number of the primary reference fuel at the audible knock limit was measured in each case. The experiments proceeded as follows:

**Step 1:** The operating conditions were established and defined using isooctane (ON 100). The parameters that define an engine operating condition are: intake manifold pressure, airflow, fuel flow, intake air temperature, coolant temperature, spark timing, and speed. The spark timing was adjusted for maximum brake torque (MBT).

**Step 2:** For each operating condition established in the first step, the octane number of the primary reference fuel supplied to the engine was decreased until audible knock occurred. This involved multiple tests run with the octane number of the primary reference fuel decreasing by approximately two numbers for each successive run. For the short time between fuel changes, the engine was motored and the fuel lines purged.

"Primary reference fuel only" tests were first completed to explore the knock trends when operating with lean mixtures and to determine baseline data, later used to understand the effects of H₂ and CO with plasmatorn-enhanced operation and hydrogen and CO addition cases.

**PLASMATRON REFORMATE ADDITION** - Tests to characterize engine knock trends in the plasmatorn engine concept were completed by replacing a fraction of the primary reference fuel and air mixture
with a H₂, CO and N₂ mixture. The plasmatron fuel reformer still being developed; so all of the experiments were carried out using bottled gas representative of the ideal output from the plasmatron when operating with gasoline. The mole fractions of H₂, CO, and N₂ in the simulated plasmatron reformate were 0.23, 0.25, and 0.52, respectively. The plasmatron fraction is defined as the fraction of total gasoline mass diverted to the plasmatron fuel reformer. For example, 30% plasmatron fraction means that 30% of the gasoline is diverted to the plasmatron, while 70% is directly injected into the engine intake port.

The relative air/fuel ratio (λ) for the plasmatron addition cases is taken for the whole system. The air, used in the plasmatron and the engine, is compared with the air required for complete oxidation of the fuel, which is entering the plasmatron fuel reformer and the engine. Since all the air and fuel eventually enter the engine, the lambda measured in the exhaust stream is the system lambda.

EQUIVALENT HYDROGEN AND CO ADDITION – The synthetic reformate used in the plasmatron cases includes both H₂ and CO. To investigate the roles of H₂ and CO independently, equivalent H₂ addition and CO addition tests were completed. To allow for a direct comparison between the plasmatron addition cases and the H₂ and CO addition cases, the corresponding equivalent H₂ and CO experiments were designed to provide the same fraction of total energy from H₂ or CO as in the plasmatron case. In this manner, the separate effects of the H₂ and CO, in the plasmatron gas, on knock could be evaluated.

EXPERIMENTAL RESULTS

GASOLINE OPERATION

Basic Trends - Figure 1 shows how the ONR changes with variations in fuel and air flows. Each node represents an engine operating condition. The number in parenthesis is the experimental primary reference fuel octane number requirement. The axes designate the fuel flow, and manifold air pressure (MAP) which is a good indication of air flow rate. Experiments of this type were carried out for two different loads and both sets of data show the same trends.

The vertical line shows that the ONR decreases with leaner operation, when the fuel flow rate is reduced at a constant inlet pressure. However, the output torque also decreases. Instead of reducing fuel to increase lambda, another approach is to increase the air flow rate and hold the flow of fuel constant.

In this case, shown by the horizontal line, the ONR increases, as well as the NIMEP, due to increasing fuel conversion efficiency when operating under leaner conditions.

To achieve constant torque (NIMEP) with leaner mixtures, a combination of less fuel and higher intake pressure is required. The ONR trend under lean operation with constant torque output is the result of two competing effects - a decrease in the ONR due to less fuel, and an increase in ONR due to higher MAP. At a more fundamental level, leaner operation increases the value of the ratio of specific heats of the unburned mixture (γu). Higher unburned mixture γ results in a higher unburned end-gas temperature at peak pressure, for the same pressure ratio, pmax/pmin. Lean mixtures have a higher γ due to reduced concentration of fuel molecules (which have lower γ than N₂ and O₂ due to their larger molecule size). For a given load, the ONR requirement increases slightly as lambda increases above approximately 1.2. The last set of data included is a series of points at constant lambda (γ = 1.5) over a range of pressures. This shows that the knock behavior of a lean mixture is highly dependent on the intake pressure.

Fig. 1 – Experimental data when operating with PRF. Values in parenthesis are octane numbers at the audible knock limit.

Role of Lambda on ONR - Figure 2 shows how the ONR and NIMEP change as a function of relative air/fuel ratio for a constant inlet pressure. This shows that a fuel leaning by 0.1 lambda results in a reduction of approximately two octane numbers. This trend compares to trends stated by Russ [10]. This is the trend with which lean operation is often associated; however, it is critical to note the NIMEP decreases along with the ONR. The decrease in ONR, and knock propensity, can be attributed to lower peak pressures, end-gas temperatures, and relative fuel concentrations.
Role of Intake Pressure on ONR - Figure 3 shows lines of constant ONR and lambda, plotted against MAP and NIMEP. As the MAP rises the NIMEP increases as well. Note that the ONR increases as the inlet pressure is raised. (4-5 ONR increase per 0.1 bar MAP). This is due to higher peak pressure and charge densities. The contours of constant ONR slope down slightly moving from near-stoichiometric to lean. The knock-limited NIMEP decreases slightly as a leaner mixture is burned.

Fig. 2 - Experimental octane number of fuel at the onset of audible knock is shown in the symbols.

Fig. 3 - Contours of lambda and octave number at audible knock.

For all operating points fueled with primary reference fuels only, the octave number at audible knock follows a clear trend with MAP, lambda, and NIMEP. Figures 4 and 5 show three-dimensional plots of ONR versus lambda and MAP. The plots resemble a plane with modest deviations. There are two prominent trends, which can be visualized by referring to Fig. 4: following a given value of MAP, one can see a tilt that shows the decrease in ONR with lean operation at constant inlet pressure. The other trend is associated with the dependence of ONR on MAP, regardless of lambda. Figure 5 shows the individual data points as well as contours of constant ONR. The top view (plan view) of this data is presented in Fig. 6. The top view maintains the axis of lambda and MAP. On this graph, the shade (color) corresponds to the ONR, in addition; contours of constant NIMEP have been added. The shades change approximately with the contours of NIMEP, which indicates, as expected, that the ONR is strongly a function of NIMEP.

Fig. 4 - ONR plotted for all data points operating primary reference fuel.

Fig. 5 - ONR plotted for all data points with primary reference fuel. Lines of constant ONR are shown as well as the individual data points.
The octane number of the primary reference fuel supplied to the engine at audible knock consistently decreases for all loads and airflow rates with plasmotron enhancement. Figures 9, 10 and 11 compare the effect of plasmotron reformate, hydrogen addition, and CO addition for each operating condition. Each figure consists of a series of lines; there is one line for each operating condition. The lines represent the measured decrease in octane number of the primary reference fuel at audible knock as the plasmotron reformate or hydrogen or CO fraction is increased.

The decrease in octane number of primary reference fuel supplied to the engine at audible knock is defined as the difference in hydrocarbon ON at the onset of knock when operating with primary reference fuels only versus the octane number of the primary reference fuel at audible knock when operating with a given plasmotron reformate fraction. A similar subtraction is done to find the decrease in octane number of primary reference fuel at knock for the H₂ and CO addition cases.

Figure 7 shows the octane number of the primary reference fuel supplied to the engine at audible knock for four operating conditions with two plasmotron reformate fractions, 15% and 30%. The primary reference fuel only case is shown for reference. In the cases where plasmotron reformate is added to the mixture, the octane number of primary reference fuel at the audible knock limit decreases. Over the range tested, the octane number of the hydrocarbon supplied at knock decreases for increasing plasmotron fractions. The equivalent graph for hydrogen addition and CO addition is shown in Fig. 8.
Figure 9 shows how the octane number of PRF at knock onset decreases for higher plasmatron reformate fractions. The benefit with plasmatron reformate is only weakly dependent on lambda and load since no clear trend is noted between the different engine operation lines. The data shows that when 15% and 30% of the fuel is partially oxidized into H₂, CO, and N₂, the octane number of the primary reference fuel required to just avoid knock decreases by about 8 ONs and 20 ONs, respectively. A similar but less substantial trend is found with pure hydrogen and with CO addition, as shown in Figs. 10 and 11, where the decrease in primary reference fuel octane number required to just avoid knock is plotted versus the fraction of the energy that was derived from hydrogen or CO. For 5% energy from H₂, the octane number of hydrocarbon fuel at the audible knock limit is 5 lower than without H₂. For 11% energy from hydrogen, there is a decrease of 10 octane numbers. For 7.1% and 14.7% energy from CO, there is a decrease in 2 octane numbers and 6 octane numbers, respectively.

Figure 12 shows the results of summing the separate H₂ and CO effects, in the proportions that these gases are present in plasmatron gas. When Fig. 12 is compared to Fig. 9, it is apparent that adding the separate effects of the H₂ and CO gives a decrease in PRF ON that is comparable to, but lower than, that observed with the plasmatron gas. Thus the CO in the plasmatron gas contributes comparably to hydrogen to lowering the octane number of primary reference fuel supplied to the engine at the onset of audible knock.

Fig. 9 - Lower octane fuel is supplied to the engine for audible knock when some energy is derived from H₂ and CO (plasmatron reformate). Data simulates 15% and 30% of the gasoline being reformed in the plasmatron fuel reformer.

Fig. 10 - Lower octane fuel is supplied to the engine for audible knock when some energy is derived from H₂. Data simulates the H₂ equivalent data for 15% and 30% of the gasoline being reformed in the plasmatron fuel reformer.

Fig. 11 - Lower octane fuel is supplied to the engine for audible knock when some energy is derived from CO. Data simulates the CO equivalent data for 15% and 30% of the gasoline being reformed in the plasmatron fuel reformer.

Fig. 12 - Sum of decreases in PRF octane number from separate H₂ and CO addition experiments corresponding to 15% and 30% of the gasoline being reformed in the plasmatron fuel reformer.
EFFECTIVE OCTANE NUMBER ESTIMATION

The aforementioned experiments show that H₂ and CO have the effect of increasing the octane number of a fuel mixture. Octane number is an empirical measure of a fuel's resistance to knock established by comparing the knock tendency of a fuel to a mixture of two primary reference fuels, isoctane and n-heptane. Results of this study show that when H₂ and CO, or a combination of H₂ and CO, are added to a gasoline-air mixture, the octane number is increased above that of the liquid hydrocarbon alone. The effects of H₂ and CO are analogous to octane-enhancing additives such as tetraethyl lead (TEL) or methyl tertiary butyl ether (MTBE). TEL and MTBE are known to increase the octane number of a mixture by an amount proportional to the mass or volume of additive mixed into a given amount of hydrocarbon fuel and that additive's octane number.

We have examined methods for estimating the octane number for blends of H₂, CO, and primary reference fuels. The approach is to calculate an average octane number based on a weighted average of the individual components' octane numbers.

Most literature estimates of the research octane number of H₂ are between 120 and 140 [11][12] [13]. This value appears reasonable when inspecting the spontaneous ignition temperature of H₂, which is significantly higher than that of isoctane, as shown in Table 2. Fuels with high knock resistance will have a high spontaneous ignition temperature; thus, H₂ should have an octane number higher than 100.

Another complication that could arise in knock testing is preignition. Hydrogen is prone to preignition, defined as ignition of the charge by a hot surface before the spark is discharged, which results from the low surface ignition energy of hydrogen. Knock tests on pure hydrogen engines must be carefully executed to ensure that the autoignition of the end-gas occurs with normal spark-ignition combustion, and not preignition.

A value for the octane number of CO has not been found in current literature. However, there are several reasons CO would have a high octane number. First, the spontaneous ignition temperature for CO is high. Secondly, this study found that CO does delay the onset of knock, when added to a primary reference fuel mixture. Discussions indicate that some recent tests, using the standard octane rating procedure, found the research octane number of CO to be 106 [11]. The octane numbers used for each pure fuel are given in Table 2.

ENERGY-WEIGHTED OCTANE NUMBER – One method for estimating an effective octane number for a fuel mixture, which is analogous to that used with primary reference fuels is to weight the octane number of each fuel component by the fraction of the energy that it represents in the cylinder. The energy-weighted effective octane number is defined in Eq. (1).

\[
ON_{\text{energy-weighted}} = \frac{\sum \left[ \left( LHV_i \times m_i \right) \times ON_i \right]}{\sum \left( LHV_i \times m_i \right)}
\]

(1)

where \( i \) is a pure fuel component, LHV is the lower heating value, and \( m_i \) is the mass flow rate of fuel \( i \).

The results from this method of octane number calculation are shown in Fig. 13. If the octane estimation method achieved perfect correlation, the data points would lie on the diagonal. The scatter shows the error; the energy-weighted octane calculation usually underestimates the octane numbers of the mixtures.

BOND-WEIGHTED OCTANE NUMBER - Hydrocarbon autoignition processes initiate with the extraction of a hydrogen atom from a fuel molecule. This fundamental process suggests an approach for estimating the effective octane number of a mixture of these fuels where the fuel proportions are weighted by the fraction of critical bonds they supply to the mixture. Critical bonds are those bonds that could take part in the spontaneous ignition process. For hydrocarbons, critical bonds are taken as the H-
\[ CRB_i = X_i \times \text{(Critical Bonds/Molecule)}_i \quad (2) \]

where \( X_i \) is the number of moles of fuel \( i \) in the mixture. The number of critical bonds originating from each pure fuel component is then multiplied by the fuels' respective octane number. Summing this product over all fuel components and dividing by the total number of critical bonds in the mixture provides a bond-weighted octane number as shown in Eq. (3).

\[ ON_{\text{bond-weighted}} = \frac{\sum (CRB \times ON_i)}{\sum CRB_i} \quad (3) \]

The results are shown in Fig. 15. The correlation is plausible. When fuel mixtures contain \( \text{H}_2 \) and \( \text{CO} \) in addition to gasoline, a method of estimating the octane number of the mixture is needed. The RMS error of the estimated octane numbers of our data set using the bond-weighting method is 1.9 octane numbers, while the RMS error using the energy-weighting method is 3.0 octane numbers.

C bonds. For example, each molecule of isooctane \((\text{C}_8\text{H}_{18})\) contributes 19 H-C bonds; hence, the tendency of these H-C bonds to break determines the probability that an isooctane-air mixture will spontaneously ignite. (It is acknowledged that the H-C bonds in isooctane do not all have the same bond energy; however, the ON includes this factor.) For \( \text{H}_2 \) to participate in the ignition reaction, 

each bond must be broken; therefore, \( \text{H}_2 \) is given a value of one critical bond per molecule. The role of \( \text{CO} \) in the ignition process is complex. A detailed chemical simulation (discussed later) shows that the presence of \( \text{CO} \) significantly reduces the \( \text{HO}_2 \) concentration, thereby changing the radical pool. The number of critical bonds in \( \text{CO} \) was determined by finding the value that resulted in the lowest error between the expected ON (mixture of PRF which knocks at the same engine condition) and the ON estimated by the bond-weighting approach. Figure 14 shows the "best-fit" number of bonds for \( \text{CO} \) is between two and three. A value of three was used for the calculations presented here. Table 3 summarizes the critical bond assumptions.

The first step to calculate the bond-weighted octane number requires finding the number of \textit{Critical Bonds} (CRB) contributed by each pure fuel \( i \) as shown in Eq. (2).

\[ \text{Table 3: Sample calculation for the critical bond weighted-octane number. Example for 15\% plasmatron reformate fraction.} \]

<table>
<thead>
<tr>
<th>Fuel</th>
<th>Moles</th>
<th>CRB/mol</th>
<th>CRB Fr.</th>
<th>Fuel ON</th>
<th>Weighted ON</th>
</tr>
</thead>
<tbody>
<tr>
<td>\text{C}<em>8\text{H}</em>{18}</td>
<td>0.233</td>
<td>18</td>
<td>0.676</td>
<td>100</td>
<td>67.6</td>
</tr>
<tr>
<td>\text{C}<em>7\text{H}</em>{16}</td>
<td>0.032</td>
<td>16</td>
<td>0.082</td>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td>\text{H}_2</td>
<td>0.349</td>
<td>1</td>
<td>0.056</td>
<td>140</td>
<td>7.8</td>
</tr>
<tr>
<td>\text{CO}</td>
<td>0.386</td>
<td>3</td>
<td>0.136</td>
<td>106</td>
<td>19.7</td>
</tr>
<tr>
<td>Total</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>95</td>
<td></td>
</tr>
</tbody>
</table>
reference fuel mixtures in a Rapid Compression Machine (RCM) [19]. The model calibration regime is similar to that of the end-gas in an SI engine.

**Physical Situation and Assumptions** - In our application, the model follows a small element of end-gas, subject to a known pressure constraint (pressure as a function of time). The calculation begins at the time of spark, where the specific volume, composition, and pressure are known. After the spark, the model assumes that the end-gas is compressed isentropically. Until autoignition, the temperature of the end-gas increases mainly due to adiabatic compression and slow chemical energy release. Other critical assumptions are:

1. Measured cylinder pressure is uniform throughout the cylinder, and therefore represents the end-gas pressure history.
2. Each cycle ingests the same amount of fuel and air, as measured by steady-state flow devices. The residual fraction in the end-gas is estimated with an improved version of the Fox correlation [22].

**Governing Equations** - To calculate the state from one time step to the next, the change in temperature \(dT\), change in the volume \(dV\), and change in number of moles \(dn\) must be determined. Pressure as a function of time is a direct input; therefore, the change in pressure is known at each model time step. The change in number of moles in the element of end-gas due to chemical reactions is calculated by chemical rate equations. The remaining parameters, which are change in temperature and volume, can be calculated by applying the energy conservation equation and ideal gas law. Equations (4)-(6) summarize the process used to arrive at \(dT\), \(dV\), and \(dn\).

\[
\frac{dn_{\text{specific}}(t)}{dt} = \text{function}(k_i, n_1...n_n) \\
\text{where} \\
k_i = \frac{A_i T^n e^{-E_i/kT}}{\rho} \\
\frac{dT}{dt} = \frac{\text{enrel}}{c_v \cdot \text{moles}} - \frac{p}{c_v \cdot \text{moles}} \frac{dV}{dt} \\
\frac{dV}{dt} = \frac{\text{moles} \cdot R_{\text{mole}} \left( \frac{dT}{dt} \right) + R_{\text{mole}} T \left( \frac{dn}{dt} \right) - V \left( \frac{dp}{dt} \right)}{p_i}
\]
Inputs to the Model – Initial conditions include: specific volume, mixture composition, and a representative individual cycle pressure history from the appropriate experiment. Specific volume at time of spark can be estimated from the crank angle of spark and the steady-state mass flows into the engine. Specie concentrations are known from the fuel composition and relative air/fuel ratio. The pressure trace that is used must be representative of a pressure cycle which experiences autoignition at the audible knock limit.

The individual cycle pressure traces at audible knock were reviewed. At the audible knock threshold, about half the pressure traces show pressure oscillations of 1 bar or higher. The pressure oscillations become apparent in the cycle near to the time of peak cylinder pressure. The cycles that show autoignition tend to be the faster burning cycles, which experience an early location of peak pressure. Data from 100 pressure cycles at audible knock were analyzed. Figure 16 illustrates how we chose a representative pressure cycle that should experience autoignition at the audible knock limit. Pressure traces that show a location of peak pressure one standard deviation earlier than the average location of peak pressure are likely to knock, and therefore are appropriate to use as input to the knock model.

![Image](image_url)

**Fig. 16** – Knock characteristics compiled for 100 pressure traces at the audible knock limit. Fast-burning pressure cycles have high likelihood of autoignition.

**Calculation Methodology** – The model was used to examine how the octave number of the primary reference fuel affected the onset of audible knock. The model was run with fuels corresponding to the experiments to see if the same trends in ONR were obtained with the model. This section describes how the ONR was determined from the model.

The model was run several times to find the ONR for one data point. For the runs, everything was held constant except the relative amounts of isoctane and n-heptane, to simulate operation with a range of octave numbers. When the reactions in the end gas become significant, the temperature rises quickly as autoignition occurs. Autoignition should first occur at peak cylinder pressure, which corresponds to peak end-gas temperature. The octave number of the fuel where autoignition occurred at peak pressure was taken as the ONR. An example of the model results is shown in Fig. 17. The figure illustrates that changes of ± 5 ON produce relatively modest shifts in time of autoignition. The simulation is only valid until autoignition. After autoignition, the pressure of the end-gas element rises rapidly, and the assumed uniform cylinder pressure is no longer a valid constraint.

![Image](image_url)

**Fig. 17** – Example and interpretation of engine knock simulation.

**Model Results** – Tables 4 and 5 show the experimental and the predicted ONR for two load cases for primary reference fuels only. There is an “offset” of about 5 ON, but the trends are comparable. Given the difficulties in describing the end-gas thermal state and complex chemistry, this offset is not surprising. However, when fuel mixtures, which include H₂ and CO are used in the model, the results no longer scale well. Even with a PRF ON of zero, knock onset with 30% plasmagron gas occurs some 5 crank angle degrees after location of maximum pressure [23].

<table>
<thead>
<tr>
<th>Relative air/fuel ratio (λ)</th>
<th>λ=1.1</th>
<th>λ=1.3</th>
<th>λ=1.5</th>
</tr>
</thead>
<tbody>
<tr>
<td>Experimental</td>
<td>88</td>
<td>90</td>
<td>93</td>
</tr>
<tr>
<td>Predicted</td>
<td>86</td>
<td>85</td>
<td>88</td>
</tr>
<tr>
<td>Difference</td>
<td>-2</td>
<td>-5</td>
<td>-5</td>
</tr>
</tbody>
</table>

| Table 4: Experimental vs predicted ONR for mid-load cases. Operating conditions are for primary reference fuels only. |
COMPREHENSIVE CHEMISTRY MODEL – A recently published detailed chemistry model for isooctane [21] was used to predict the effects of H₂ and CO addition on autoignition times. H₂ and CO are formed and consumed in the break-up reactions of isooctane; therefore, initial fuel blends containing H₂ and CO should be valid inputs to the model. To evaluate the chemical effects due to mixture composition, constant volume calculations were performed. The simulation results illustrated in Fig. 18 show constant volume predictive runs, each beginning at 875 K and 45 bar corresponding to typical conditions at peak pressure in the cylinder. For each mixture, the relative air-fuel ratio was 1.5. The plasmatron reformate case simulates 30% of the gasoline being diverted to the plasmatron. The isooctane + H₂ case matches the H₂ energy fraction (10%) in the plasmatron case. In the isooctane + CO case, the CO energy fraction matches the CO energy fraction (15%) in the plasmatron case.

![Fig. 18 - Ignition delays for four fuel mixtures in a constant volume simulation as predicted by a comprehensive chemistry model.](image)

The results show that CO and H₂, both separately and together, lengthen the ignition delay. Addition of CO to isooctane-air mixture lengthens the ignition delay by 0.5 ms. H₂ added to isooctane-air mixture lengthens the ignition delay by 3 ms. The effect of adding H₂, CO, and N₂ to isooctane-air mixture shows the longest ignition delay ~ 5 ms longer than the isooctane only case. These trends correspond to the experimental data trends, which show the same relative ranking for CO, H₂, and plasmatron gas addition. It should be noted, however, that in the engine experiments the maximum end-gas temperature does vary somewhat with these fuel changes; see discussion below. The reduced chemistry models run at the same condition for isooctane predict ignition delays of approximately half of those of the comprehensive models [23].

DISCUSSION

This work has shown that knock trends associated with lean operation depend on what parameters are held constant as the mixture is made leaner. If leaner operation is achieved by decreasing fuel flow, while holding airflow constant, the knock tendency of the engine decreases, along with the torque output. This trend of decreasing knock tendency with leaner mixtures, similar to what is displayed in Gruden and Hahn’s work [6], is a result of less reactive end-gas mixtures and lower peak end-gas temperatures due to lower peak pressures. Holding fuel flow constant, and introducing more air to achieve a leaner mixture increases the knock tendency of the engine significantly, as well as engine output because peak temperatures and pressures rise. To achieve constant torque with leaner operation, the air flow must be substantially increased and the fuel flow slightly decreased. In this constant torque scenario, knock tendency increases slightly with increasing leanness. These results imply that a lean engine, boosted to maintain constant torque, is less resistant to knock than a naturally aspirated stoichiometric engine at the same torque output.

Estimates of end-gas temperature help explain this last trend. The end-gas can be modeled as a homogeneous mixture, which experiences an isentropic compression. Comparing stoichiometric and lean engine operating conditions at constant torque shows that lean unburned mixtures could reach higher maximum temperatures based on the relevant peak pressures and pressure ratios. The isentropic relation, Eq. (7) and Table 6 illustrate the effect of a higher ratio of specific heats, γ₂, as occurs in lean mixtures,

\[
\left( \frac{p_2}{p_1} \right)^{\frac{\gamma_2 - 1}{\gamma_2}} = \frac{T_2}{T_1}
\]

where state 1 is the start of compression and state 2 is the point of maximum pressure. Note that changes in the fuel composition also vary γ₂ due to change PRF fuel concentration in the overall fuel mixture.
Table 6: Isentropic compression calculation for constant output operation, with stoichiometric and lean mixtures.

<table>
<thead>
<tr>
<th>Lambda</th>
<th>$T_1$ [K]</th>
<th>$P_1$ [bar]</th>
<th>$P_2$ [bar]</th>
<th>$\gamma_0$</th>
<th>$\Delta T$ [K]</th>
<th>$T_2$ [K]</th>
</tr>
</thead>
<tbody>
<tr>
<td>1.0</td>
<td>340</td>
<td>1.1</td>
<td>49</td>
<td>1.33</td>
<td>877</td>
<td></td>
</tr>
<tr>
<td>1.5</td>
<td>340</td>
<td>1.3</td>
<td>53</td>
<td>1.35</td>
<td>889</td>
<td></td>
</tr>
</tbody>
</table>

That the end-gas in a lean mixture reaches a higher temperature due to compression than a stoichiometric mixture is consistent with findings by researchers at Chalmers and Lund Universities [24]. The researchers found that leaner mixtures reach the critical temperature at a lower compression than richer mixtures. As a consequence, leaner mixtures will autoignite earlier, which results in a higher knock intensity.

Experiments show that $\text{H}_2$ and CO have an octane-enhancing effect when added to hydrocarbon/fair mixtures. The knock changes that occur when $\text{H}_2$ and CO are added to the mixture result from several effects. The dominant effect is slowing of the ignition reactions in the end-gas with the addition of $\text{H}_2$ and CO. Thus, when these fuels are added to a hydrocarbon blend, they increase the octane number of the overall mixture. The effective mixture ON can be estimated from summing a bond-weighted component ON. Experiments with $\text{H}_2$ addition, and CO addition, show the same trends of increasing the knock resistance of the mixture. The benefits of the plasmatron gas mixture ($\text{H}_2$, CO, $\text{N}_2$) are greater than but comparable to the addition of the separate $\text{H}_2$ and CO effects. The $\text{H}_2$ addition effect is larger than the CO effect.

**CONCLUSIONS**

The main conclusions that can be drawn from this work are summarized below:

While operating the engine at constant net indicated mean effective pressure, leaner mixtures are more likely to knock due primarily to their higher ratio of specific heats than stoichiometric mixtures, which increases the end-gas temperature rise during compression – from intake to peak pressure. Operating with increasingly lean mixtures, while maintaining engine torque constant, requires an increase in manifold intake pressure, which also slightly increases the octane number requirement.

$\text{H}_2$ and CO have high octane numbers and therefore increase the overall octane number of the fuel mixture when blended with primary reference fuels. An effective octane number can be calculated by a bond-weighted average of individual fuels' octane numbers. The octane benefits from $\text{H}_2$ and CO do not appear to vary substantially with load or relative air/fuel ratio.

A reduced chemistry autoignition model was used to model a small element of end-gas as it follows a specified pressure profile with time. Autoignition is assumed to have occurred when end-gas temperature rises rapidly due to chemical energy release. Predicted autoignition trends for primary reference fuels agree with the experimental data.

A comprehensive chemistry model was used to investigate the autoignition delay times for various fuel mixtures in a constant volume situation where initial conditions were similar to that of the end-gas at peak pressure. The fuel mixtures run in the simulation were primary reference fuels alone, and with the addition of plasmatron reformate, and $\text{H}_2$ and CO separately. The comprehensive chemical mechanism predicts relative autoignition delay times that agree with the trend shown in the experimental results.

$\text{H}_2$ and CO inhibit knock by slowing autoignition chemistry and slightly increasing flame speed. In vehicles with onboard reforming the octane number of the fuel mixture that would reach the engine is higher. For example, if 15% of the fuel is reform to $\text{H}_2$ and CO, the resulting fuel mixture will be approximately 10 octane numbers higher than the original HC fuel. Based on previous research relating a change in compression ratio to octane requirements (e.g. Russ and Chevron [10][25]), an increase in 10 octane numbers would permit an increase of two compression ratios.

**ACKNOWLEDGMENTS**

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**REFERENCES**


